

> restart

>

PROBLEMA DEL ARCO Y LA FLECHA

> restart

$$\begin{aligned} > \text{Hooke} := \left(\frac{\left(\frac{11}{\left(\frac{30}{100} \right)} \right)}{\left(\frac{16}{\left(\frac{1000}{\left(\frac{981}{100} \right)} \right)} \right)} \right); \text{MasaFlecha} := \left(\frac{\left(\frac{16}{\left(\frac{1000}{\left(\frac{981}{100} \right)} \right)} \right)}{\left(\frac{16}{\left(\frac{1000}{\left(\frac{981}{100} \right)} \right)} \right)} \right) \\ & \text{Hooke} := \frac{110}{3} \end{aligned}$$

$$\text{MasaFlecha} := \frac{8}{4905} \quad (1)$$

> Ecua := -Hooke·s(t) = MasaFlecha·diff(s(t), t\$2); evalf(%, 3)

$$\text{Ecua} := -\frac{110 s(t)}{3} = \frac{8 \frac{d^2}{dt^2} s(t)}{4905}$$

$$-36.7 s(t) = 0.00163 \frac{d^2}{dt^2} s(t) \quad (2)$$

> EcuaDos := (rhs(Ecua) - lhs(Ecua)) = 0; evalf(%, 3)

$$\text{EcuaDos} := \frac{d^2}{dt^2} s(t) + \frac{89925 s(t)}{4} = 0$$

$$\frac{d^2}{dt^2} s(t) + 22500. s(t) = 0. \quad (3)$$

> CondIni := s(0) = -\frac{36}{100}, D(s)(0) = 0

$$\text{CondIni} := s(0) = -\frac{9}{25}, D(s)(0) = 0 \quad (4)$$

> SolGral := dsolve(EcuaDos); evalf(%, 3)

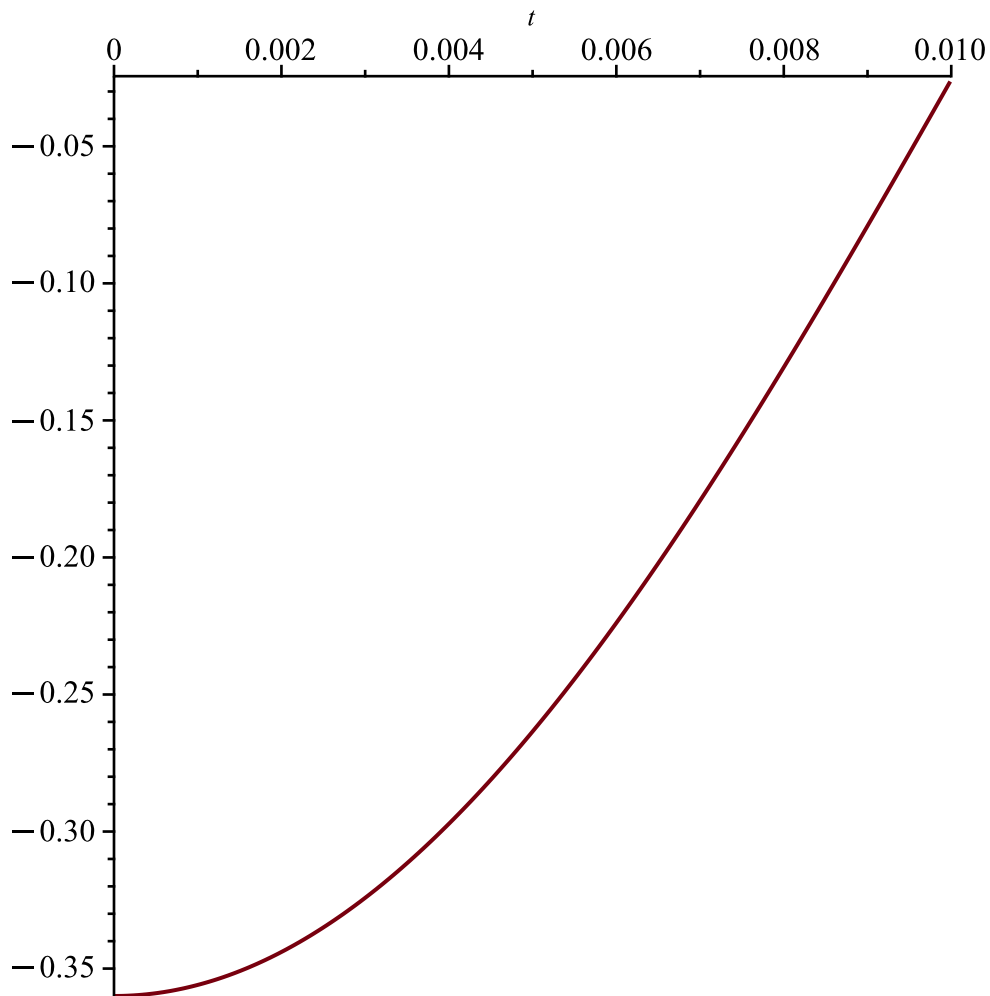
$$\text{SolGral} := s(t) = c_1 \sin\left(\frac{5\sqrt{3597} t}{2}\right) + c_2 \cos\left(\frac{5\sqrt{3597} t}{2}\right)$$

$$s(t) = c_1 \sin(150. t) + c_2 \cos(150. t) \quad (5)$$

> SolPart := dsolve({EcuaDos, CondIni}) : evalf(%, 3)

$$s(t) = -0.360 \cos(150. t) \quad (6)$$

> plot(rhs(SolPart), t=0..0.01)



> $Tiempo := solve(rhs(SolPart) = 0) : evalf(\%, 6)$
0.0104763 (7)

> $Velocidad := subs(t = Tiempo, rhs(diff(SolPart, t))) : evalf(\%, 3); \frac{evalf(\%, 3) \cdot 3600}{1000}$

$$Velocidad := \frac{9 \sqrt{3597} \sin\left(\frac{\pi}{2}\right)}{10}$$
54.0
194.4000000 (8)

VUELO LIBRE FLECHA

> $EcuaVertical := diff(y(t), t\$2) = -\frac{981}{100}$

$$EcuaVertical := \frac{d^2}{dt^2} y(t) = -\frac{981}{100}$$
 (9)

> $EcuaHorizontal := diff(x(t), t) = Velocidad \cdot \cos\left(\frac{\pi}{4}\right)$

$$EcuaHorizontal := \frac{d}{dt} x(t) = \frac{9 \sqrt{3597} \sqrt{2}}{20}$$
 (10)

$$\begin{aligned} &> \text{CondVertical} := y(0) = 2, D(y)(0) = \text{Velocidad} \cdot \sin\left(\frac{\text{Pi}}{4}\right) \\ &\quad \text{CondVertical} := y(0) = 2, D(y)(0) = \frac{9\sqrt{3597}\sqrt{2}}{20} \end{aligned} \quad (11)$$

$$\begin{aligned} &> \text{CondHoriz} := x(0) = 5 \\ &\quad \text{CondHoriz} := x(0) = 5 \end{aligned} \quad (12)$$

$$\begin{aligned} &> \text{SolVertical} := \text{dsolve}(\{\text{EcuaVertical}, \text{CondVertical}\}) : \text{evalf}(\%, 3) \\ &\quad y(t) = -4.90 t^2 + 38.2 t + 2. \end{aligned} \quad (13)$$

$$\begin{aligned} &> \text{SolHorizontal} := \text{dsolve}(\{\text{EcuaHorizontal}, \text{CondHoriz}\}) : \text{evalf}(\%, 3) \\ &\quad x(t) = 38.2 t + 5. \end{aligned} \quad (14)$$

$$\begin{aligned} &> \text{TiempoVuelo} := \text{solve}(\text{rhs}(\text{SolVertical}) = 0); \text{evalf}(\%, 3) \\ &\quad \text{TiempoVuelo} := \frac{5\sqrt{7194}}{109} - \frac{5\sqrt{66490}}{327}, \frac{5\sqrt{7194}}{109} + \frac{5\sqrt{66490}}{327} \\ &\quad \quad -0.06, 7.84 \end{aligned} \quad (15)$$

$$\begin{aligned} &> \text{DistanciaFinal} := \text{subs}(t = \text{TiempoVuelo}[2], \text{rhs}(\text{SolHorizontal})); \text{evalf}(\%, 3) \\ &\quad \text{DistanciaFinal} := \frac{9\sqrt{7194} \left(\frac{5\sqrt{7194}}{109} + \frac{5\sqrt{66490}}{327} \right)}{20} + 5 \\ &\quad \quad 304. \end{aligned} \quad (16)$$

$$\begin{aligned} &> \text{TiempoAlturaMaxima} := \text{solve}(\text{rhs}(\text{diff}(\text{SolVertical}, t)) = 0); \text{evalf}(\%, 3) \\ &\quad \text{TiempoAlturaMaxima} := \frac{5\sqrt{7194}}{109} \\ &\quad \quad 3.89 \end{aligned} \quad (17)$$

$$\begin{aligned} &> \text{AlturaMaxima} := \text{subs}(t = \text{TiempoAlturaMaxima}, \text{rhs}(\text{SolVertical})); \text{evalf}(\%, 3) \\ &\quad \text{AlturaMaxima} := \frac{305}{4} \\ &\quad \quad 76.2 \end{aligned} \quad (18)$$

$$> \text{plot}([\text{rhs}(\text{SolHorizontal}), \text{rhs}(\text{SolVertical}), t = 0 .. \text{TiempoVuelo}[2]], \text{scaling} = \text{CONSTRAINED})$$

